

Inputs used in *Predictions of selected flavour observables within the SM*

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We have presented predictions of selected flavour observables within the Standard Model in ref. [1]. We gather here the inputs used for these predictions, including those that could not be listed for lack of space. Most of them come from lattice gauge theories and are obtained following our usual averaging method, described in more detail in Sec. 3.

1 Inputs for the CKM fit

In tables 1 and 2, we provide the experimental and theoretical inputs required for the global fit described in Sec. I of ref. [1].

| Observable | Value and uncertainties | Reference |
|---|---|-----------|
| $ V_{ud} _{\text{nucl}}$ | 0.97425 ± 0.00022 | [2] |
| $ V_{us} _{\text{semi}} f_+(0)$ | 0.2163 ± 0.0005 | [3] |
| $\mathcal{B}(K \rightarrow e\nu_e)$ | $(1.584 \pm 0.0020) \cdot 10^{-5}$ | [4] |
| $\mathcal{B}(K \rightarrow \mu\nu_\mu)$ | 0.6347 ± 0.0018 | [3] |
| $\mathcal{B}(\tau \rightarrow K\nu_\tau)$ | 0.00696 ± 0.00023 | [4] |
| $\frac{\mathcal{B}(K \rightarrow \mu\nu_\mu)}{\mathcal{B}(\pi \rightarrow \mu\nu_\mu)}$ | $(1.3344 \pm 0.0041) \cdot 10^{-2}$ | [3] |
| $\frac{\mathcal{B}(\tau \rightarrow K\nu_\tau)}{\mathcal{B}(\tau \rightarrow \pi\nu_\tau)}$ | $(6.53 \pm 0.11) \cdot 10^{-2}$ | [5] |
| $\mathcal{B}(D \rightarrow \mu\nu)$ | $(3.82 \pm 0.32 \pm 0.09) \cdot 10^{-4}$ | [6] |
| $\mathcal{B}(D_s \rightarrow \tau\nu)$ | $(5.29 \pm 0.28) \cdot 10^{-2}$ | [7] |
| $\mathcal{B}(D_s \rightarrow \mu\nu_\mu)$ | $(5.90 \pm 0.33) \cdot 10^{-3}$ | [7] |
| $ V_{ub} _{\text{semi}}$ | $(3.92 \pm 0.09 \pm 0.45) \cdot 10^{-3}$ | [7] |
| $\mathcal{B}(B \rightarrow \tau\nu)$ | $(1.68 \pm 0.31) \cdot 10^{-4}$ | [8] |
| $ V_{cb} _{\text{semi}}$ | $(40.89 \pm 0.38 \pm 0.59) \cdot 10^{-3}$ | [7] |
| $B \rightarrow \pi\pi, \rho\pi, \rho\rho$ | Branching ratios, CP asymmetries | [7] |
| $\sin(2\beta)_{[c\bar{c}]}$ | 0.678 ± 0.020 | [7] |
| $B \rightarrow D^{(*)}K^{(*)}$ | Inputs for GGSZ, GLW, ADS methods | [7] |
| Δm_d | $0.507 \pm 0.005 \text{ ps}^{-1}$ | [7] |
| Δm_s | $17.77 \pm 0.12 \text{ ps}^{-1}$ | [9] |
| $ \epsilon_K $ | $(2.229 \pm 0.010) \cdot 10^{-3}$ | [4] |

Table 1: Experimental inputs used for the global fit of ref. [1]. The errors were treated as Gaussian (if there is only a statistical uncertainty) or using the Rfit scheme (if both statistical and systematic uncertainties are present).

| Theoretical parameter | Value and uncertainties | Reference |
|-------------------------------|---|-----------|
| $f_+(0)$ | $0.9632 \pm 0.0028 \pm 0.0051$ | Sec. 3 |
| f_K | $156.3 \pm 0.3 \pm 1.9$ MeV | Sec. 3 |
| f_K/f_π | $1.205 \pm 0.001 \pm 0.010$ | Sec. 3 |
| f_{D_s}/f_D | $1.186 \pm 0.005 \pm 0.010$ | Sec. 3 |
| f_{D_s} | $251.3 \pm 1.2 \pm 4.5$ MeV | Sec. 3 |
| f_{B_s} | $231 \pm 3 \pm 15$ MeV | Sec. 3 |
| f_{B_s}/f_B | $1.209 \pm 0.007 \pm 0.023$ | Sec. 3 |
| $\hat{B}_{B_s}/\hat{B}_{B_d}$ | $1.01 \pm 0.01 \pm 0.03$ | Sec. 3 |
| \hat{B}_{B_s} | $1.28 \pm 0.02 \pm 0.03$ | Sec. 3 |
| \hat{B}_K | $0.730 \pm 0.004 \pm 0.036$ | Sec. 3 |
| κ_ϵ | $0.940 \pm 0.013 \pm 0.023$ | [10] |
| $\bar{m}_c(\bar{m}_c)$ | $(1.286 \pm 0.013 \pm 0.040)$ GeV | [10] |
| $\bar{m}_t(\bar{m}_t)$ | $(165.017 \pm 1.156 \pm 0.11)$ GeV | [10] |
| $\alpha_s(M_Z)$ | 0.1176 ± 0.0020 | [4] |
| η_{cc} | computed from $\bar{m}_c(\bar{m}_c)$ and α_s | [11] |
| η_{ct} | 0.47 ± 0.04 | [12] |
| η_{tt} | 0.5765 ± 0.0065 | [13] |
| $\hat{\eta}_B$ | 0.8393 ± 0.0034 | [10] |

Table 2: Theoretical inputs used for the global fit of ref. [1]. The errors were treated using the Rfit scheme.

| Theoretical parameter | Value and uncertainties | Reference |
|---|---------------------------|-----------|
| $\tilde{\mathcal{B}}_{S,B_s}/\tilde{\mathcal{B}}_{S,B_d}$ | $1.01 \pm 0 \pm 0.03$ | [14] |
| $\tilde{\mathcal{B}}_{S,B_s}(m_b)$ | $0.91 \pm 0.03 \pm 0.12$ | [14] |
| $\overline{m}_s(\overline{m}_b)$ | (0.085 ± 0.017) GeV | [16] |
| $\overline{m}_b(\overline{m}_b)$ | (4.248 ± 0.051) GeV | [7] |
| m_b^{pow} | $(4.7 \pm 0 \pm 0.1)$ GeV | [16] |
| \mathcal{B}_{R_0} | 1.0 ± 0.5 | [16] |
| $\mathcal{B}_{\tilde{R}_1}$ | 1.0 ± 0.5 | [16] |
| \mathcal{B}_{R_1} | 1.0 ± 0.5 | [16] |
| $\mathcal{B}_{\tilde{R}_2}$ | $1.0 \pm 0 \pm 0.5$ | [16] |
| $\mathcal{B}_{\tilde{R}_3}$ | $1.0 \pm 0 \pm 0.5$ | [16] |

Table 3: Theoretical inputs used for the predictions of ref. [1] concerning neutral-meson mixing. The errors were treated using the Rfit scheme.

2 Inputs for the predictions in the Standard Model

In tables 3 and 4, we collect the additional theoretical inputs required for the predictions of flavour quantities in the Standard Model described in Sec. I of ref. [1]. We do not recall the elements for the parametrisation of $B \rightarrow X_s \gamma$, which is described in detailed in ref. [15].

3 Lattice inputs

3.1 Averaging method

Several hadronic inputs are required for the fits presented by CKMfitter, and we mostly rely on lattice QCD simulations to estimate these quantities. The presence of results from different collaborations with various statistics and systematics make it all the more necessary to combine them in a careful way.

We collect the relevant calculations of the quantity that we are interested in: we take only unquenched results with 2 or 2+1 dynamical fermions, even those from proceedings without a companion article. In these results, we separate the error estimates into a Gaussian part and a flat part that is treated à la Rfit. The Gaussian part collects the uncertainties from purely statistical origin, but also the systematics that can be controlled and treated in a similar way (e.g., interpolation or fitting in some cases). The remaining systematics constitute the Rfit error. If there are several sources of error in the Rfit category, we add them linearly ¹.

The Rfit model is simple but also very strict. It amounts to assuming that the theoretical uncertainty is rigorously constrained by a mathematical bound that is our only piece of information. If Rfit is taken stricto sensu and the individual likelihoods are combined in the usual way (by multiplication), the final uncertainty can be underestimated, in particular in the case of marginally compatible values. We correct this effect by adopting the following averaging recipe. The central value is obtained by combining the whole likelihoods. Then we combine the Gaussian uncertainties by combining likelihoods restricted to their Gaussian part. Finally we assign to this combination the smallest of the individual Rfit uncertainties. The underlying idea is twofold:

¹keeping in mind that in many papers in the literature, this combination is done in quadrature and the splitting between different sources is not published.

| Theoretical parameter | Value and uncertainties | Reference |
|---|--------------------------------------|-----------|
| $\mu_{B \rightarrow \ell\ell}$ | 200 ± 120 GeV | [17] |
| $m_s(2 \text{ GeV})$ | 0.1 ± 0.02 GeV | [18] |
| μ_b | 6 ± 3.6 GeV | [18] |
| \bar{m}_b | 4.2 | [18] |
| $\lambda_B(\mu_h)$ | 0.51 ± 0.12 GeV | [18] |
| $\lambda_{B_s}(\mu_h)$ | 0.6 ± 0.2 | [18] |
| f_{\perp, K^*} | 0.185 ± 0.010 | [18] |
| a_{1, \perp, K^*} | 0.04 ± 0.03 | [18] |
| a_{2, \perp, K^*} | 0.15 ± 0.1 | [18] |
| $T_1^{B \rightarrow K^*}(0)$ | 0.31 ± 0.04 | [18] |
| $f_{\perp, \phi}$ | 0.186 ± 0.009 | [18] |
| $a_{2, \perp, \phi}$ | 0.2 ± 0.2 | [18] |
| $\xi_{B_s \rightarrow \phi}$ | 1.01 ± 0.13 | [18] |
| $G_V + G_A$ | -0.24 ± 0.06 | [18] |
| $G_V - G_A$ | -0.03 ± 0.015 | [18] |
| $l_c - \tilde{l}_c(B \rightarrow K^*)$ | 0.000242 ± 0.000370 | [18] |
| $l_c + \tilde{l}_c(B \rightarrow K^*)$ | -0.000952 ± 0.000800 | [18] |
| $l_c - \tilde{l}_c(B_s \rightarrow \phi)$ | 0.000306 ± 0.000320 | [18] |
| $l_c + \tilde{l}_c(B_s \rightarrow \phi)$ | -0.000930 ± 0.000750 | [18] |
| $l_u - \tilde{l}_u(B \rightarrow K^*)$ | -0.000099 ± 0.000300 | [18] |
| $l_u + \tilde{l}_u(B \rightarrow K^*)$ | 0.001172 ± 0.000821 | [18] |
| $l_u - \tilde{l}_u(B_s \rightarrow \phi)$ | -0.000581 ± 0.000300 | [18] |
| $l_u + \tilde{l}_u(B_s \rightarrow \phi)$ | 0.000893 ± 0.000625 | [18] |
| δP_{cu} | 0.04 ± 0.02 | [19] |
| Δ_{EM} | -0.003 | [19] |
| κ_+ | $(0.5173 \pm 0.0025) \cdot 10^{-10}$ | [19] |
| κ_L | $(2.231 \pm 0.013) \cdot 10^{-10}$ | [19] |
| κ_{10} | 1.6624 | [20] |
| κ_{01} | -2.3537 | [20] |
| κ_{11} | -1.5862 | [20] |
| κ_{20} | 1.5036 | [20] |
| κ_{02} | -4.3477 | [20] |

Table 4: Theoretical inputs used for the predictions of ref. [1] concerning radiative B decays and rare K decays. The errors were treated using the Rfit scheme.

- the present state of art cannot allow us to reach a better theoretical accuracy than the best of all estimates
- this best estimate should not be penalized by less precise methods (as it would happen be the case if one would take the dispersion of the individual central values as a guess of the combined theoretical uncertainty).

It should be stressed that the concept of a theoretical uncertainty is ill-defined, and the combination of them even more. Thus our approach is only one among the alternatives that can be found in the literature. In contrast to some of the latter, ours is algorithmic and can be reproduced.

3.2 Decay constants and form factors

f_K

| Reference | Article | N_f | Mean | Stat | Syst |
|-------------|---------|-------|-------|------|------------------|
| ETMC09 | [21] | 2 | 158.1 | 0.8 | 3.1 |
| MILC07 | [22] | 2+1 | 156.5 | 0.4 | $^{+1.0}_{-2.7}$ |
| HPQCD07 | [23] | 2+1 | 157 | 0.6 | 3.3 |
| ALVdW08 | [24] | 2+1 | 153.9 | 1.7 | 6.5 |
| Our average | | | 156.3 | 0.3 | 1.9 |

f_K/f_π

| Reference | Article | N_f | Mean | Stat | Syst |
|-------------|---------|-------|-------|--------|----------------------|
| ETMC09 | [21] | 2 | 1.210 | 0.006 | 0.024 |
| MILC07 | [22] | 2+1 | 1.197 | 0.003 | $^{+0.006}_{-0.013}$ |
| NPLQCD07 | [25] | 2+1 | 1.218 | 0.002 | $^{+0.024}_{-0.011}$ |
| HPQCD07 | [23] | 2+1 | 1.189 | 0.002 | 0.014 |
| ALVdW08 | [24] | 2+1 | 1.191 | 0.016 | 0.026 |
| BMW10 | [26] | 2+1 | 1.192 | 0.010 | 0.019 |
| Our average | | | 1.205 | 0.0012 | 0.0095 |

f_{D_s}

| Reference | Article | N_f | Mean | Stat | Syst |
|-------------|---------|-------|-------|------|----------------|
| CP-PACS00 | [27] | 2 | 267 | 13 | $^{+27}_{-17}$ |
| MILC02 | [28] | 2 | 241 | 5 | $^{+41}_{-30}$ |
| ETMC09 | [21] | 2 | 244 | 3 | 9 |
| HPQCD03 | [29] | 2+1 | 290 | 20 | 64 |
| FNAL-MILC09 | [30] | 2+1 | 260 | 6.8 | 14 |
| HPQCD10 | [47] | 2+1 | 248.0 | 1.4 | 4.5 |
| Our average | | | 251.3 | 1.2 | 4.5 |

f_{D_s}/f_D

| Reference | Article | N_f | Mean | Stat | Syst |
|-------------|---------|-------|-------|-------|----------------------|
| CP-PACS00 | [27] | 2 | 1.182 | 0.039 | $^{+0.087}_{-0.046}$ |
| MILC02 | [28] | 2 | 1.14 | 0.01 | $^{+0.06}_{-0.07}$ |
| ETMC09 | [21] | 2 | 1.24 | 0.03 | 0.01 |
| HPQCD07 | [23] | 2+1 | 1.164 | 0.006 | 0.020 |
| FNAL-MILC09 | [30] | 2+1 | 1.200 | 0.016 | 0.025 |
| Our average | | | 1.186 | 0.005 | 0.010 |

f_{B_s}

| Reference | Article | N_f | Mean | Stat | Syst |
|-------------|---------|-------|------|------|----------------|
| CP-PACS01 | [31] | 2 | 242 | 9 | $+^{53}_{-34}$ |
| MILC02 | [28] | 2 | 217 | 6 | $+^{58}_{-31}$ |
| JLQCD03 | [32] | 2 | 215 | 9 | $+^{19}_{-15}$ |
| ETMC09 | [45] | 2 | 243 | 6 | 15 |
| HPQCD03 | [29] | 2+1 | 260 | 7 | 39 |
| FNAL-MILC09 | [33] | 2+1 | 243 | 6 | 22 |
| HPQCD09 | [34] | 2+1 | 231 | 5 | 30 |
| Our average | | | 231 | 3 | 15 |

f_{B_s}/f_B

| Reference | Article | N_f | Mean | Stat | Syst |
|-------------|---------|-------|-------|-------|--------------------|
| CP-PACS01 | [31] | 2 | 1.179 | 0.018 | 0.023 |
| MILC02 | [28] | 2 | 1.16 | 0.01 | $+^{0.08}_{-0.04}$ |
| JLQCD03 | [32] | 2 | 1.13 | 0.03 | $+^{0.17}_{-0.02}$ |
| ETMC09 | [45] | 2 | 1.27 | 0.03 | 0.04 |
| FNAL-MILC09 | [33] | 2+1 | 1.245 | 0.028 | 0.049 |
| HPQCD09 | [34] | 2+1 | 1.226 | 0.020 | 0.033 |
| RBC/UKQCD10 | [46] | 2+1 | 1.15 | 0.05 | 0.20 |
| Our average | | | 1.209 | 0.007 | 0.023 |

$f_+(0)$ for $K \rightarrow \pi \ell \nu$

| Reference | Article | N_f | Mean | Stat | Syst |
|-------------|---------|-------|--------|--------|------------------------|
| RBC06 | [35] | 2 | 0.968 | 0.009 | 0.006 |
| ETMC09 | [36] | 2 | 0.9560 | 0.0057 | 0.0127 |
| RBC-UKQCD10 | [50] | 2+1 | 0.9599 | 0.0034 | $+^{0.0045}_{-0.0057}$ |
| Our average | | | 0.9632 | 0.0028 | 0.0051 |

3.3 Meson mixing

$B_K^{\text{MS}}(2\text{GeV})$

| Reference | Article | N_f | Mean | Stat | Syst |
|--|---------|-------|-------|-------|-------|
| JLQCD08 | [38] | 2 | 0.537 | 0.004 | 0.072 |
| ETMC 10 | [51] | 2 | 0.532 | 0.019 | 0.026 |
| HPQCD/UKQCD06 | [39] | 2+1 | 0.618 | 0.018 | 0.179 |
| ALVdW09 | [41] | 2+1 | 0.527 | 0.006 | 0.049 |
| RBC/UKQCD07 | [40] | 2+1 | 0.524 | 0.010 | 0.052 |
| BSW10 | [49] | 2+1 | 0.526 | 0.008 | 0.040 |
| Our average for $B_K^{\text{MS}}(2\text{GeV})$ | | | 0.532 | 0.003 | 0.026 |
| Our average for \hat{B}_K | | | 0.730 | 0.004 | 0.036 |

\hat{B}_{B_s}

| Reference | Article | N_f | Mean | Stat | Syst |
|-------------|---------|-------|-------|-------|----------------------|
| JLQCD03 | [32] | 2 | 1.299 | 0.034 | $+0.122$ -0.095 |
| HPQCD06 | [42] | 2+1 | 1.168 | 0.105 | 0.140 |
| RBC/UKQCD07 | [43] | 2+1 | 1.21 | 0.05 | 0.05 |
| HPQCD09 | [34] | 2+1 | 1.326 | 0.04 | 0.03 |
| Our average | | | 1.28 | 0.02 | 0.03 |

$\hat{B}_{B_s}/\hat{B}_{B_d}$

| Reference | Article | N_f | Mean | Stat | Syst |
|-------------|---------|-------|-------|-------|----------------------|
| JLQCD03 | [32] | 2 | 1.017 | 0.016 | $+0.076$ -0.017 |
| HPQCD09 | [34] | 2+1 | 1.053 | 0.02 | 0.03 |
| RBC/UKQCD10 | [46] | 2+1 | 0.96 | 0.02 | 0.03 |
| Our average | | | 1.01 | 0.01 | 0.03 |

Refs. [34] and [46] provide only ξ and f_{B_s}/f_{B_d} . We have extracted $\hat{B}_{B_s}/\hat{B}_{B_d}$ in both cases assuming a total correlation in the systematics of ξ and $\hat{B}_{B_s}/\hat{B}_{B_d}$.

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